A PARSIMONIOUS MACROECONOMIC MODEL FOR ASSET PRICING

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I study asset prices in a two-agent macroeconomic model with two key features: limited stock market participation and heterogeneity in the elasticity of intertemporal substitution in consumption (EIS). The model is consistent with some prominent features of asset prices, such as a high equity premium, relatively smooth interest rates, procyclical stock prices, and countercyclical variation in the equity premium, its volatility, and in the Sharpe ratio. In this model, the risk-free asset market plays a central role by allowing non-stockholders (with low EIS) to smooth the fluctuations in their labor income. This process concentrates non-stockholders' labor income risk among a small group of stockholders, who then demand a high premium for bearing the aggregate equity risk. Furthermore, this mechanism is consistent with the very small share of aggregate wealth held by non-stockholders in the U.S. data, which has proved problematic for previous models with limited participation. I show that this large wealth inequality is also important for the model's ability to generate a countercyclical equity premium. When it comes to business cycle performance, the model's progress has been more limited: consumption is still too volatile compared to the data, whereas investment is still too smooth. These are important areas for potential improvement in this framework.

KEYWORDS: Equity premium puzzle, limited stock market participation, elasticity of intertemporal substitution, wealth inequality, Epstein–Zin preferences.

1. INTRODUCTION

SINCE THE 1980s, a vast body of empirical research has documented some interesting and puzzling features of asset prices. For example, Mehra and Prescott (1985) showed that the equity premium observed in the historical U.S. data was hard to reconcile with a canonical consumption-based asset pricing model and, as it later turned out, with many of its extensions. A parallel literature in financial economics found that the equity premium is predictable by a number of variables including the dividend yield, challenging the longheld view that stock returns follow a martingale (Campbell and Shiller (1988)). Other studies have documented that the expected equity premium, its volatility, and the ratio of the two—the conditional Sharpe ratio—move over time

¹For helpful conversations and comments, I thank Daron Acemoglu, John Campbell, V. V. Chari, Jeremy Greenwood, Lars Hansen, Urban Jermann, Narayana Kocherlakota, Per Krusell, Martin Lettau, Debbie Lucas, Sydney Ludvigson, Rajnish Mehra, Martin Schneider, Tony Smith, Kjetil Storesletten, Ivan Werning, Amir Yaron, and, especially, a co-editor and five anonymous referees, as well as seminar participants at Duke University (Fuqua), Massachusetts Institute of Technology, Ohio State University, University of Montréal, University of Pittsburgh, University of Rochester, UT-Austin, UT-Dallas, NBER Economic Fluctuations and Growth Meetings, NBER Asset Pricing Meetings, the SED Conference, and the AEA Winter Meetings. Financial support from the National Science Foundation under Grant SES-0351001 is gratefully acknowledged. The usual disclaimer applies.

DOI: 10.3982/ECTA6658

following a countercyclical business cycle pattern (Schwert (1989) and Chou, Engle, and Kane (1992)).

In this paper, I ask if these asset pricing phenomena can be explained in a parsimonious macroeconomic model with two key features: limited participation in the stock market and heterogeneity in the elasticity of intertemporal substitution in consumption (EIS). The limited nature of stock market participation and the concentration of stock wealth even among stockholders is well documented. For example, until the 1990s more than two-thirds of U.S. households did not own any stocks at all, while the richest 1% held 48% of all stocks (Poterba and Samwick (1995) and Investment Company Institute (2002)). As for the heterogeneity in preferences, the empirical evidence that I review in Section 3 indicates that stockholders have a higher EIS than non-stockholders. The interaction of these two features is important, as will become clear below.

I choose the real business cycle model as the foundation that I build upon to provide a contrast with the poor asset pricing implications of that framework that are well known; this helps to highlight the role of the new features considered in this paper. Specifically, I study an economy with competitive markets and a neoclassical production technology subject to capital adjustment costs. There are two types of agents. The majority of households (first type) do not participate in the stock market where claims to the firm's future dividend stream are traded. However, a risk-free bond is available to all households, so non-stockholders can also accumulate wealth and smooth consumption intertemporally. Finally, consistent with empirical evidence, non-stockholders are assumed to have a low EIS, whereas stockholders have a higher elasticity. To clarify the role played by different preference parameters, I employ Epstein–Zin preferences and disentangle risk aversion from the EIS. I find that heterogeneity in risk aversion plays no essential role, whereas heterogeneity in the EIS (and especially the low EIS of non-stockholders) is essential for the results of this paper.

I first examine a benchmark version of the model in which labor supply is inelastic. The calibrated model is consistent with some salient features of asset prices, such as a high equity premium with a plausible volatility, and a low average interest rate. Furthermore, the variability of the interest rate is very low in the U.S. data, which has proved challenging to explain for some previous models that have otherwise successful implications. The standard deviation of the risk-free rate is about 4%–6.5% in the present model, which is still higher than in the U.S. data, but quite low compared to some of these earlier studies. So, the present paper provides a step in the right direction as far as interest rate volatility is concerned.

Although there are now several papers that have made progress in explaining these unconditional moments in the context of production economies,² some

²Jermann (1998), Boldrin, Christiano, and Fisher (2001), Danthine and Donaldson (2002), Storesletten, Telmer, and Yaron (2007), and Uhlig (2006), among others.

aspects of asset price dynamics have proved more difficult to generate. The present model is consistent with the procyclical variation in stock prices, the mean reversion in the equity premium, and the countercyclical variation in the expected equity premium, in its volatility, and in the conditional Sharpe ratio. While the model also reproduces the long-horizon predictability of the equity premium, the degree of predictability is quantitatively small compared to the data.

This paper, as well as earlier models with limited participation, builds on the empirical observation, first made by Mankiw and Zeldes (1991), that stockholders' consumption growth is more volatile (and more highly correlated with returns) than that of non-stockholders. Therefore, a high equity premium can be consistent with the relatively smooth per capita consumption process in the U.S. data, since stockholders only make up a small fraction of the population. Existing theoretical models differ precisely in the economic mechanisms they propose for generating this high volatility of stockholders' consumption growth.

The mechanism in this paper differs from earlier studies (most notably, Saito (1995) and Basak and Cuoco (1998)) in some crucial ways. In particular, in these earlier models, non-stockholders consume out of wealth, which they must invest in the bond market given the absence of any other investment opportunity. As a result, each period stockholders make interest payments to non-stockholders, which leverages the capital income of stockholders, thereby amplifying their consumption volatility. Although this is a potentially powerful mechanism, it only works quantitatively if these interest payments are substantial, which in turn requires non-stockholders to own a substantial fraction of aggregate wealth. But, in reality, non-stockholders own only one-tenth of aggregate wealth in the United States, and this counterfactual implication has been an important criticism raised against these models.

One contribution of this paper is to propose a new economic mechanism that avoids this counterfactual implication. Specifically, the mechanism results from the interaction of three factors. First, non-stockholders receive labor income every period, which is *stochastic*, and trade in the bond market to smooth the fluctuations in their consumption. Second, because of their low EIS, non-stockholders have a stronger desire for consumption smoothing and therefore need the bond market much more—than stockholders (who have a higher EIS and an additional asset for consumption smoothing purposes). However, and third, since the source of risk is aggregate, the bond market cannot eliminate this risk and merely reallocates it across agents. In equilibrium, stockholders make payments to non-stockholders in a countercyclical fashion, which serves to smooth the consumption of non-stockholders and amplifies the volatility of stockholders, who then demand a large premium for holding aggregate risk. As shown in Section 6.3, this mechanism is consistent with a very small wealth share of non-stockholders precisely because it is the cyclical nature of interest payments that is key, and not their average amount (which can very well be zero).

The same mechanism also explains why the equity premium is countercyclical. Essentially, because non-stockholders have very low wealth, they become effectively more risk averse during recessions when their wealth falls even further (because with incomplete markets, value functions have more curvature at low wealth levels). This is not the case for stockholders who hold substantially more wealth. Consequently, during recessions, non-stockholders demand more consumption smoothing, which strengthens the mechanism described above (i.e., increased trade in the bond market, more volatile consumption growth for stockholders), generating a higher premium in recessions. In Section 5, I quantify the contribution of these channels to both the level and the countercyclicality of the equity premium.

I also investigate the extent to which labor supply choice can be endogenized without compromising overall performance. Cobb–Douglas utility does not appear to be suitable for this task: it results in a deterioration of asset pricing results and generates labor hours much smoother than in the data. One reason for these results is that these preferences do not allow an independent calibration of the EIS and the Frisch labor supply elasticity, which are both crucial for my analysis. This poor performance perhaps does not come as a surprise in light of the earlier findings: for example, Lettau and Uhlig (2000), Boldrin, Christiano, and Fisher (2001, hereafter BCF), and Uhlig (2006) uncovered various problems generated by endogenous labor supply in asset pricing models and identified certain labor market frictions that successfully overcome these difficulties. Incorporating the same frictions into the model with Cobb–Douglas utility could also improve its performance, although this is beyond the scope of the present paper.

Next I consider the utility specification first introduced by Greenwood, Hercowitz, and Huffman (1988, GHH) and find that it performs better: it preserves the plausible asset pricing implications of the model with inelastic labor fairly well and it generates business cycle implications in the same ballpark as existing macroeconomic models. While these results suggest that GHH preferences could provide a promising direction for endogenizing labor supply in this class of models, there is still much room for improvement: consumption volatility remains significantly higher than in the U.S. data, whereas investment volatility is still too low. Therefore, the progress made by this model has been rather limited in tackling these well-known shortcomings shared by many macro-based asset pricing models. A potentially fruitful approach could be to introduce certain labor market frictions, such as wage rigidities, that have been found to improve asset pricing models along these dimensions (Uhlig (2006)).

This paper is related to a growing literature that builds models for jointly studying asset prices and macroeconomic behavior. In addition to the papers cited in footnote 2, Danthine and Donaldson (2002) constructed an entrepreneur—worker model, in which the worker lives hand-to-mouth and there is no labor supply choice. In this environment, labor contracts between the two agents act as "operational leverage" and affect asset prices in a way

that is similar to limited participation. Storesletten, Telmer, and Yaron (2007) built a heterogeneous-agent model and showed that persistent idiosyncratic shocks with countercyclical innovation variance generate plausible unconditional moments. As noted earlier, one difference in my paper is the focus on the dynamics of asset prices, which is not studied in these papers. Finally, in terms of integrating recursive preferences into macro-based asset pricing models, an important precursor is Tallarini (2000), who showed how one can fix the EIS and increase the risk aversion in the standard real business cycle (RBC) model to generate a high market price of risk without causing a deterioration in business cycle properties. The present paper goes one step further by introducing limited participation, preference heterogeneity, and adjustment costs, and generates a high equity premium with a risk aversion that is much lower than in Tallarini (2000). Other notable contributions that are contemporaneous with the present paper include Campanale, Castro, and Clementi (2007) and Gomes and Michaelides (2008), who built full blown macro-based asset pricing models with recursive preferences, and Uhlig (2007), who provided a convenient log-linear framework for asset pricing with recursive preferences, labor–leisure choice, and long-run risk. I further discuss some of these papers

The paper is organized as follows. The next section presents the model, and the parametrization is discussed in Section 3. Sections 4 and 5 contain the asset pricing results and the mechanism. The macroeconomic implications are presented in Section 6; Section 7 concludes.

2. THE MODEL

Households

The economy is populated by two types of agents who live forever. The population is constant and is normalized to unity. Let $\mu \in (0,1)$ denote the measure of the second type of agents (who will be called stockholders later). Consumers are endowed with one unit of time every period, which they allocate between market work and leisure. I consider three different preference specifications in this paper that can be written as special cases of the Epstein–Zin recursive utility function

(1)
$$U_t^i = \left[(1 - \beta) u^i(c_t, 1 - l_t) + \beta \left(E_t (U_{t+1}^i)^{1 - \alpha^i} \right)^{(1 - \rho^i)/(1 - \alpha^i)} \right]^{1/(1 - \rho^i)}$$

for i=h, n, where throughout the paper the superscripts h and n denote $\mathrm{stock} h$ olders and n on-stockholders, respectively, and c and l denote consumption and labor supply, respectively. For the parametrizations I consider below, the risk aversion parameter for static wealth gambles will be proportional to α^i , and the EIS will be *inversely* proportional to ρ^i , although the precise relationship will also depend on the choice of u. As indicated by the superscripts, the two types are allowed to differ in their preference parameters.

It should be emphasized that the choice of recursive preferences is made mainly for clarity: by disentangling risk aversion from the elasticity of intertemporal substitution, these preferences allow us to examine the impact of heterogeneity in the EIS on asset prices without generating corresponding differences in risk aversion that could confound the inference.^{3,4}

The Firm

There is an aggregate firm that produces a single consumption good using capital (K_t) and labor (L_t) inputs according to a Cobb–Douglas technology: $Y_t = Z_t K_t^{\theta} L_t^{1-\theta}$, where $\theta \in (0,1)$ is the factor share parameter. The technology level evolves according to

$$\log(Z_{t+1}) = \phi \log(Z_t) + \varepsilon_{t+1}, \quad \varepsilon \stackrel{\text{i.i.d.}}{\sim} N(0, \sigma_{\varepsilon}^2).$$

The firm's managers maximize the value of the firm, which equals the value of the future dividend stream generated by the firm, $\{D_{t+j}\}_{j=1}^{\infty}$, discounted by the marginal rate of substitution process of firm owners, $\{\beta^{j} \frac{\Lambda_{t+j}}{\Lambda_{t}}\}_{j=1}^{\infty}$. Specifically, the firm's problem is

(2)
$$P_t^s = \max_{\{I_{t+j}, L_{t+j}\}} E_t \left[\sum_{j=1}^{\infty} \beta^j \frac{\Lambda_{t+j}}{\Lambda_t} D_{t+j} \right]$$

subject to the law of motion for capital, which features "adjustment costs" in investment:

(3)
$$K_{t+1} = (1 - \delta)K_t + \Phi\left(\frac{I_t}{K_t}\right)K_t.$$

 P_t^s is the ex-dividend value of the firm, and I normalize the number of shares outstanding to unity (for convenience) so that P_t^s is also the stock price. The adjustment cost function $\Phi(\cdot)$ is concave in investment, which captures the difficulty of quickly changing the level of capital installed in the firm.

³This expositional advantage notwithstanding, the ability to calibrate risk aversion and EIS separately is not essential for the main substantive results of the paper. This can be seen by comparing the results reported here to the working paper version (Guvenen (2006)), which uses constant relative risk aversion (CRRA) preferences.

⁴Habit preferences also break the reciprocal relation between the relative risk aversion (RRA) and EIS parameters. However, as is well known, these preferences can generate a high equity premium even in a simple RBC model with inelastic labor supply and capital adjustment costs (Jermann (1998)). Therefore, using habit in the present model would confound the mechanisms created by habit with those studied here (e.g., resulting from limited participation). Having said that, given the popularity of habit preferences in the recent business cycle research (see, e.g., Christiano, Eichenbaum, and Evans (2005)), future work should explore the implications of a model that combines habit formation with limited stock market participation.

Every period the firm sells one-period bonds, at price P_t^f , to finance part of its investment. The total supply of these bonds is constant over time and equals a fraction, χ , of the average capital stock owned by the firm (as in Jermann (1998), Danthine and Donaldson (2002)). As a result, the firm makes net interest payments in each period in the amount of $(1 - P_t^f)\chi \overline{K}$ to bond owners.⁵ An equity share in this firm entitles its owner to the entire stream of future dividends, which is given by the profits net of wages, investment, and interest payments: $D_t = Z_t K_t^\theta L_t^{1-\theta} - W_t L_t - I_t - (1 - P_t^f)\chi \overline{K}$.

Financial Markets

In this economy, the firm's equity shares (stocks) and one-period bonds issued by the firm are traded. The difference between the two groups is in their investment opportunity sets: the "non-stockholders" can freely trade the risk-free bond, but they are restricted from participating in the stock market. The "stockholders," on the other hand, have access to both markets and hence are the sole capital owners in the economy. Finally, I impose portfolio constraints as a convenient way to prevent Ponzi schemes.

Individuals' Dynamic Problem and the Equilibrium

In a given period, the portfolio of each group can be expressed in terms of the *beginning-of-period* capital stock, K, the aggregate bond holdings of non-stockholders *after* production, B, and the technology level, Z. Let Y denote the aggregate state vector (K, B, Z). The dynamic programming problem of a stockholder can be expressed as

(4)
$$V^{h}(\omega; \mathbf{Y}) = \max_{c,l,b',s'} [(1-\beta)u(c, 1-l) + \beta (E[V^{h}(\omega'; \mathbf{Y}')|Z]^{1-\alpha^{i}})^{(1-\rho^{i})/(1-\alpha^{i})}]^{1/(1-\rho^{i})}$$

s.t.

(5)
$$c + P^f(\mathbf{Y})b' + P^s(\mathbf{Y})s' \le \omega + W(K, Z)l,$$

(6)
$$\omega' = b' + s'(P^s(Y') + D(Y')),$$

(7)
$$K' = \Gamma_K(\mathbf{Y}), \quad B' = \Gamma_B(\mathbf{Y}),$$

$$(8) b' \geq \underline{B},$$

⁵The introduction of corporate debt into this framework allows me to model bonds as a positive net supply asset, which is more realistic. However, the Modigliani–Miller theorem holds in this framework in the sense that stockholders are able to fully undo the effect of leverage in their portfolio. Therefore, the existence of leverage has no effect on quantity allocations, which I have verified by solving the model without leverage.

where ω denotes financial wealth, b' and s' are individual bond and stock holdings, respectively, Γ_K and Γ_B denote the laws of motion for the wealth distribution which are determined in equilibrium, and P^f is the equilibrium bond pricing function. The problem of a non-stockholder can be written as above with $s' \equiv 0$, and the superscript h replaced with n. Finally, the stock return and the risk-free rate are defined as usual: $R^s = (P^{s'} + D')/P^s - 1$ and $R^f = 1/P^f - 1$, and the equity premium is denoted by $R^{ep} \equiv R^s - R^f$.

A stationary recursive competitive equilibrium for this economy is given by a pair of value functions, $V^i(\omega^i; Y)$, i = h, n; consumption, labor supply, and bond holding decision rules for each type of agent, $c^i(\omega^i; Y)$, $l^i(\omega^i; Y)$, and $b^{ir}(\omega^i; Y)$; a stockholding decision rule for stockholders, $s'(\omega^h; Y)$; stock and bond pricing functions, $P^s(Y)$ and $P^f(Y)$; a competitive wage function, W(K, Z); an investment function for the firm, I(Y); laws of motion for aggregate capital and the aggregate bond holdings of non-stockholders, $\Gamma_K(Y)$ and $\Gamma_B(Y)$; and a marginal utility process, $\Lambda(Y)$, for the firm owners, such that the following statements hold:

- (i) Given the pricing functions and the laws of motion, the value function and decision rules of each agent solve that agent's dynamic problem.
- (ii) Given W(K, Z) and the equilibrium discount rate process obtained from $\Lambda(Y)$, the investment function, I(Y), and the labor choice of the firm, L(Y), are optimal.
- (iii) All markets clear: (a) $\mu b^{h'}(\varpi^h; Y) + (1 \mu)b^{n'}(\varpi^n; Y) = \chi \overline{K}/P^f(Y)$ (bond market), (b) $\mu s'(\varpi^h; Y) = 1$ (stock market), and (c) $L(Y) = \mu l^h(\varpi^h; Y) + (1 \mu)l^n(\varpi^n; Y)$ (labor market), where ϖ^i denotes the wealth of each type of agent in state Y in equilibrium.
- (iv) Aggregate laws of motion are consistent with individual behavior: $K' = (1 \delta)K + \Phi(I(Y)/K)K$ and $B' = (1 \mu)b^n(\varpi^n, Y)$.
- (v) There exists an invariant probability measure ${\bf P}$ defined over the ergodic set of equilibrium distributions.

3. QUANTITATIVE ANALYSIS

The solution to the recursive competitive equilibrium is obtained using numerical methods. In addition to the well-known challenges associated with solving incomplete markets asset pricing models (cf. Krusell and Smith (1997) and Storesletten, Telmer, and Yaron (2007)), the present model is further complicated by the presence of (i) capital adjustment costs, (ii) Epstein–Zin preferences, and (iii) leverage. These features raise a number of issues that we now discuss.

First, because markets are incomplete, one cannot solve for allocations first and then obtain prices as is typically done in representative agent models. Instead, allocations and pricing functions must be solved simultaneously. Second, the three features mentioned above introduce important nonlinearities into equilibrium functions, making it essential to start the algorithm with good initial guesses and update them very slowly. Third, asset prices are well known to be more sensitive to approximation errors (much more so than quantity allocations). Furthermore, some key variables in the model exhibit significant volatility and are, therefore, not confined to narrow regions of the state space, so the accuracy of local (e.g., log-linear, etc.) approximations is not always easy to ensure. So, instead, I approximate the equilibrium functions over the entire state space using multi-dimensional cubic splines and check that equilibrium conditions ((i)-(v) at the end of Section 2) are satisfied at all grid points. Finally, the wealth distribution (which is a relevant state vector in this model) is not approximated by moments as done by Krusell and Smith (1997), but instead its evolution is tracked exactly via the functions Γ_K and Γ_B . Of course, this is only feasible here because there are two types of agents, so the wealth distribution has only two dimensions. Overall, the algorithm I use trades speed for precision and is, therefore, not very fast, but does deliver accurate results.

I now provide an outline of the algorithm for the baseline model with inelastic labor supply introduced in Section 3.1, which contains all the essential components. A supplemental computational appendix (Guvenen (2010)) contains further details.

Step 0—Initialization: Choose appropriate grids for ω^h , ω^n (each agent's wealth holdings), and Y. Off-grid values for all functions are obtained by cubic spline interpolation. Initial guesses for equilibrium functions are obtained by solving a simplified version of the model with no adjustment costs ($\xi = \infty$), with no leverage ($\chi = 0$), and with CRRA utility ($\alpha = \rho$). The algorithm for this simplified model is essentially the same as Steps 1–5 below (with no need for Step 2(c) because $P^s \equiv K$), but is much more stable. Let superscript j index the iteration number. Set i = 1 and start the iteration:

Step 1—Solve Each Agent's Dynamic Problem (defined by equations (4)– (8)): These are standard Bellman equations and are solved via value function iteration. The fact that preferences are of the Epstein-Zin form poses no additional difficulty in this step—in fact, it makes it *easier* in certain ways. More on this in the appendix.

Step 2—Update Equilibrium Functions: Λ^{j-1} , I^{j-1} , D^{j-1} , $P^{s,j-1}$, Γ_K^j .

- (a) Use $c^{h,j}(\omega; Y)$ and $V^{h,j}(\omega; Y)$ obtained in Step 1 to construct $\frac{A^{j}(Y')}{A^{j}(Y)}$. Using this stochastic discount factor, solve the firm's problem ((2) and (3)) to obtain $I^{j}(\mathbf{Y})$.
- (b) Obtain $D^j(Y) = ZK^{\theta}L^{1-\theta} WL I^j(Y) (1 P^{f,j-1}(Y))\chi \overline{K}$ and up-
- date $\Gamma_K^j(\boldsymbol{Y})$: $K' = (1 \delta)K + \Phi(I^j(\boldsymbol{Y})/K)K$. (c) Define the temporary variable $\widetilde{P}^0(\boldsymbol{Y}) \equiv P^{s,j-1}(\boldsymbol{Y})$. Now iterate for $m = 1, \ldots, M$: $\widetilde{P}^m(\boldsymbol{Y}) = E[\beta \Lambda^j(\boldsymbol{Y}, Z')(D^j(\boldsymbol{Y}') + \widetilde{P}^{m-1}(\boldsymbol{Y}')) \mid \boldsymbol{Y}]$. Set $P^{s,j}(\boldsymbol{Y}) = \sum_{i=1}^{m} (P^i(\boldsymbol{Y}) + P^{m-1}(\boldsymbol{Y}')) \mid \boldsymbol{Y}$. $\widetilde{P}^{M}(\mathbf{Y})$.

Step 3—Update the Bond Pricing Function, $P^{f,j-1}$: The method here follows Krusell and Smith (1997) closely. First, solve

$$\begin{split} \widetilde{V}^{h}(\boldsymbol{\omega}; \boldsymbol{Y}, \widehat{q}) \\ &= \max_{b', s'} \left((1 - \beta) c^{1-\rho} + \beta \left(E[V^{h, j}(\boldsymbol{\omega}'; \boldsymbol{Y}')^{1-\alpha} | \boldsymbol{Y}] \right)^{(1-\rho)/(1-\alpha)} \right)^{1/(1-\rho)} \\ \text{s.t.} \quad c + \widehat{q}b' + P^{s, j}(\boldsymbol{Y})s' \leq \boldsymbol{\omega} + W(K, Z) \end{split}$$

and equations (6)–(8) (and with $s' \equiv 0$ for the non-stockholder). The only difference between this problem and the individual's original Bellman equation is that here the individual views the current period bond price as some arbitrary parameter \widehat{q} , which is not necessarily equal to $P^{f,j-1}(Y)$. This problem generates bond holding rules $\widetilde{b}^h(\omega; Y, \widehat{q})$ and $\widetilde{b}^n(\omega; Y, \widehat{q})$ which explicitly depend on \widehat{q} . Then, at each grid point, search over values of \widehat{q} to find q^* such that the bond market clears, that is, excess demand is less than 10^{-8} . Then set $P^{f,j}(Y) = q^*(Y)$.

Step 4: Obtain
$$\Gamma_B^j(Y)$$
: $B'(Y) = (1 - \mu)\widetilde{b}^n(\varpi^n, Y, q^*(Y))$.

Step 5: Iterate on Steps 1–4 until convergence. I require maximum percentage discrepancy (across all points in the state space) between consecutive iterations to be less than 10^{-6} for P^f , 10^{-4} for P^s , and 10^{-6} for aggregate laws of motion. Further tightening these convergence criteria has no noticeable effect.

As further described in the appendix, additional checks are conducted to ensure the accuracy of the solution. For example, one should also test whether the stock market clears at all state points, which is not explicitly imposed by the algorithm above. It indeed does: the maximum $|\mu s'(\varpi^h; Y) - 1| < 10^{-5}$. Another useful check is to see whether increasing the number of grid points changes the results: doubling the number of points in ω and K directions and tripling them in the B direction (simultaneously) had no noticeable effect on the statistics studied in the paper. Further details are provided in the supplementary computational appendix (Guvenen (2010)).

3.1. Baseline Parametrization

A model period corresponds to 1 month of calendar time to approximate the frequent trading in financial markets. Because asset pricing statistics are typically reported at annual frequencies and macroeconomic statistics are reported at quarterly frequencies, I aggregate financial variables and quantities to their respective reporting frequencies to calculate the relevant statistics as explained below. Table I summarizes the baseline parameter choices.

The capital share parameter, θ , is set to 0.3. The functional form for Φ is specified as $a_1(I_t/K_t)^{1-1/\xi} + a_2$, as in Jermann (1998), where a_1 and a_2 are constants chosen such that the steady state level of capital is invariant to ξ . The curvature parameter ξ determines the severity of adjustment costs. As ξ approaches infinity, Φ becomes linear, and investment is converted into capital

	TABLE I
BASELINE	PARAMETRIZATION ^a

Parameter	'arameter		
Calibrated Outside	the Model		
$oldsymbol{eta}^*$	Time discount rate	0.99	
$1/\rho^h$	EIS of stockholders	0.3	
$1/\rho^n$	EIS of non-stockholders	0.1	
μ	Participation rate	0.2	
$oldsymbol{\phi}^*$	Persistence of aggregate shock	0.95	
$\dot{ heta}$	Capital share	0.30	
ξ	Adjustment cost coefficient	0.40	
δ^*	Depreciation rate	0.02	
<u>B</u>	Borrowing limit	$6\overline{W}$	
$\overline{\chi}$	Leverage ratio	0.15	
Calibrated Inside th	ne Model (to Match Targets)		
$\sigma_arepsilon^*$	Standard deviation of shock (%)	1.5/1.5/1.	
$\alpha^{\tilde{h}} = \alpha^n$	Relative risk aversion	6	

^aThe asterisks indicate that the reported value refers to the implied quarterly value for a parameter that is calibrated to monthly frequency. \overline{W} is the average monthly wage rate in the economy. The last two parameters are chosen (i) to match the standard deviation of Hodrick–Prescott filtered output in quarterly data (1.89%) and (ii) to generate an annual Sharpe ratio of 0.25. The standard deviation values refer to CONS/CD/GHH models, respectively.

one for one (frictionless economy limit). At the other extreme, as ξ approaches zero, Φ becomes a constant function and the capital stock remains constant regardless of the investment level (exchange economy limit). I set $\xi = 0.40$, which is broadly consistent with the values reported in the empirical literature (see Christiano and Fisher (1998) for a survey of existing estimates). Because there is also a fair amount of disagreement about the correct value of ξ , in Section 6.2, I also conduct sensitivity analysis with respect to this parameter. The calibration of the capital accumulation equation is completed by setting δ to 0.0066, implying a quarterly depreciation rate of 2%. As for the technology shock, I match the first order autocorrelation of 0.95 of the Solow residuals at quarterly frequencies by setting $\phi = 0.976$ at monthly frequency. I discretize the AR(1) process for Z_t using a 15-state Markov process. The innovation standard deviation, σ_{ε} , is set later below.

Given the absence of idiosyncratic shocks in the present model, it does not seem realistic for borrowing constraints to bind frequently for entire groups of population. Therefore, in the baseline case I calibrate these constraints to be quite loose—equal to 6 months of labor income for both types of agents—which almost never bind in the simulations. As for the calibration of the leverage ratio, Masulis (1988, Table 1.3) reported that the leverage ratio (debt/book

⁶In the supplementary appendix, I show that if constraints were tight enough to bind frequently, if anything, this raises the equity premium.

value) of U.S. firms has varied between 13% and 44% from 1929 to 1986. With my calibration, the leverage ratio in the model is set to 15% of the average equity value and fluctuates between 11% and 32%. Moreover, this calibration also ensures that the firm is always able to pay its interest obligations, so the corporate bond is default-free.

Participation Rates

The model assumes a constant participation rate in the stock market, which seems to be a reasonable approximation for the period before the 1990s when the participation rate was either stable or increasing gradually (Poterba and Samwick (1995, Table 7)). In contrast, during the 1990s participation increased substantially: from 1989 to 2002 the number of households who owned stocks increased by 74%; by 2002, half of U.S. households had become stock owners (Investment Company Institute (2002)). Modeling the participation boom in this later period would require going beyond the stationary structure of the present model, so instead, I exclude this later period (1992–present) both when calibrating the participation rate and when comparing the model to the data. I set the participation rate in the model, μ , to 20%, roughly corresponding to the average rate from 1962 to 1992 (a period during which participation data are available). Note that even during times when participation was higher, households in the top 20% have consistently owned more than 98% of stocks (Poterba and Samwick (1995, Table 9)).

Utility Functions

I consider three different specifications for the period utility function. First, to provide a simple and well-known benchmark, I begin with the case where labor supply is inelastic (i.e., leisure is not valued) and assume that the period utility function is of the standard power form: $u(c, 1-l) = c^{1-\rho^i}$. This is a useful benchmark that allows a direct comparison to the existing literature where inelastic labor supply is the most common assumption. In addition, this case allows us to illustrate the key mechanisms that result from limited participation in their simplest form. To distinguish between different versions of the model, I will refer to this case as the CONS model.

The remaining two specifications feature valued leisure for a full-blown quantitative analysis. The first one features a Cobb–Douglas function (hereafter, the CD model) commonly used in macroeconomic analysis: $u(c, 1-l) = (c^{\gamma}(1-l)^{1-\gamma})^{1-\rho^i}$. However, one restrictive property of this functional form is that ρ^i and γ jointly pin down the EIS, the fraction of time devoted to market work, and the Frisch labor supply elasticity. In other words, choosing the two parameters to match the first two empirical magnitudes automatically pins down the Frisch elasticity, which is a serious restriction given that we are interested in constructing a model that allows us to study macroeconomic quantities and asset prices jointly. To overcome this difficulty I use a third utility function:

 $u(c, 1-l) = (c - \psi(l^{1+\gamma})/(1+\gamma))^{1-\rho^i}$, introduced by Greenwood, Hercowitz, and Huffman (1988, hereafter the GHH model). This specification has three distinct parameters that can be chosen to separately target the three parameters mentioned above. This feature will be useful in the analysis that follows.

Preference Parameters

There is a large body of empirical work that documents heterogeneity in the EIS across the population (see Guvenen (2006) for a more comprehensive review of the empirical evidence). These studies find that, by and large, non-stockholders (and the poor, in general) have an elasticity of substitution that is very low—close to zero—while stockholders (and the wealthy, in general) have an EIS that is higher. For example, Blundell, Browning, and Meghir (1994) estimated that households in the top income quintile have an EIS that is three times that of households in the bottom quintile of the distribution. Similarly, Barsky, Juster, Kimball, and Shapiro (1997) estimated the distribution of the EIS parameter in the population and found the average to be below 0.2, but also found the highest percentiles to be exceeding unit elasticity.

One theoretical explanation for this observed heterogeneity was provided by Browning and Crossley (2000). They started with a model of choice where agents consume several goods with different income elasticities. Because the budget share of luxuries rises with wealth, the aggregate consumption bundle of wealthy individuals has more goods with high income elasticities than that of poor individuals. Browning and Crossley (2000) proved that this observation also implies that luxuries are easier to *postpone* than necessities and, consequently, that the EIS (with respect to total consumption) increases with wealth. Since stockholders are substantially wealthier than non-stockholders, this also implies heterogeneity in the EIS across these two groups as found in these studies. To broadly capture the empirical evidence described above, I set the EIS of non-stockholders to 0.1 and assume an EIS that is three times higher (0.3) for stockholders (in all versions of the model). Finally, I set β equal to 0.9966 (monthly) so as to match the U.S. capital–output ratio of 2.5 in annual data.

⁷Although in this paper I do not explicitly model the source of the heterogeneity in the EIS (so as not to add another layer of complexity), one way to do this would be by assuming nonhomothetic preferences following Browning and Crossley's analysis. Specifically, suppose that both agents have *identical* utility functions that feature "benchmark consumption levels": $u_t^i = (c_t^i - a\overline{C}_t)^{1-\rho}/(1-\rho)$, where \overline{C}_t is aggregate consumption. With this specification, the EIS is rising with the consumption (and, therefore, the wealth) of an individual. Furthermore, wealth inequality in this framework is mainly due to limited participation and is quite robust to changes in the curvature of the utility of both agents (see Guvenen (2006) for a detailed analysis of this point). Therefore, with these preferences, stockholders continue to be much wealthier and, consequently, consume more than non-stockholders. By choosing ρ and a appropriately, one can generate the same EIS values assumed (exogenously) in the present paper. The supplemental appendix presents the details of such a calibration that broadly generates the same asset pricing results as in the CONS model.

With Cobb–Douglas preferences, there is only one additional parameter, γ , which is chosen to match the average time devoted to market activities (0.36 of discretionary time). I continue to keep the EIS values of both groups as above. However, as noted above, γ and ρ^i also determine the Frisch labor supply elasticity, which means that assuming heterogeneity in the EIS also implies unintended heterogeneity in the Frisch elasticity: 1.35 for stockholders and 0.69 for non-stockholders. Although such heterogeneity is difficult to justify with any empirical evidence I am aware of, there seems to be no practical way to get around this problem with CD preferences; I will return to this caveat later.

The GHH specification provides more flexibility, with one additional parameter. The Frisch elasticity is now equal to $1/\gamma$ for both types of agents, which I set equal to 1. This value is consistent with the estimates reported in Kimball and Shapiro (2003). However, there is a fair degree of disagreement in the literature about the correct value of this parameter, so I also discuss below the effect of different values for γ on the results. The average hours worked is given by $\overline{L} = (\overline{W}(\kappa)/((1+\gamma)\kappa))^{1/\gamma}$, where $\overline{W}(\kappa)$ is the average wage rate in the economy whose dependence on κ is made explicit. For a target value of $\overline{L} = 0.36$, this equation is solved to obtain the required value of κ .

The existing empirical evidence on the risk aversion parameter is much less precise than one would like. Moreover, the limited evidence available pertains to the population average, whereas what will matter for asset prices in this framework is the risk aversion of stockholders, who constitute only a small fraction of the population, making those average figures even less relevant. Therefore, I calibrate the risk aversion of stockholders indirectly, that is, by matching the model to some empirical targets. (I also conduct a sensitivity analysis in Section 6.2.)

Specifically, I first consider the CONS model. I choose the two parameters that are free at this point $(\alpha^h, \sigma_\varepsilon)$ to match two empirical targets: (i) the volatility of Hodrick–Prescott filtered quarterly output (1.89%) and (ii) an annual Sharpe ratio of 0.25. I then set the risk aversion of non-stockholders equal to the same value. My target value for the Sharpe ratio is somewhat lower than the 0.32 figure in the U.S. data (Table II). This is because forcing the model to explain the full magnitude of the risk premium is likely to come at the expense of poor performance in other areas, such as macroeconomic behavior or asset price dynamics, which I am also interested in analyzing. The present choice is intended to balance these different considerations.

For practical considerations, I restrict the parameter search to integer values in the α^h direction (from 2 to 10) and consider 0.1 increments in the σ_ε direction (from 0.1% to 2%). I minimize an equally weighted quadratic objective written in the percent deviation from each empirical target. The minimum is obtained for $\sigma_\varepsilon = 1.5\%$ (quarterly standard deviation) for the CONS model with $\alpha^h = 6$. For the CD and GHH models, I keep the risk aversion parameter at this value and choose σ_ε in each case to match output volatility. The

27.1

26.9

19.1

2.44

	U.S. Data		CONS	Model	
$\alpha^h, \alpha^n \\ 1/\rho^h, 1/\rho^n$		6/6 0.3/0.1	6/6 0.3/ 0.3	6/6 0.1 /0.1	6/ 12 0.3/0.1
	A. Stoo	ck and Bond Ret	urns		
$E(R^{\mathrm{ep}})$	6.17 (1.99)	5.46	2.44	7.65	5.52
$\sigma(R^{\mathrm{ep}})$	19.4 (1.41)	21.9	15.3	27.2	22.0
$\sigma(R^s)$	19.3 (1.38)	20.6	14.7	27.0	20.8
$E(R^{\rm ep})/\sigma(R^{\rm ep})$	0.32 (0.11)	0.25^{a}	0.16	0.28	0.25
$E(R^f)$	1.94 (0.54)	1.31	3.20	0.24	1.35
$\sigma(R^f)$	5.44 (0.62)	6.65	4.55	8.52	6.71

 $E(P^s/D)$

 $\sigma(\Delta \log D)$

 $\frac{\sigma(\Delta \log c^h)}{\sigma(\Delta \log c^n)}$

 $\sigma(\log(P^s/D))$

TABLE II Unconditional Moments of Asset Returns: Model With Inelastic Labor Supply

B. Price-Dividend Ratio

27.2

26.6

19.1

C. Consumption Growth Volatility

2.42

25.9

13.8

14.0

0.78

29.5

38.7

24.2

1.12

22.1 (0.58)

26.3 (1.67)

13.4 (0.94)

 $>1.5-2.0^{b}$

resulting values are $\sigma_{\varepsilon} = 1.5\%$ in the CD model and $\sigma_{\varepsilon} = 1.1\%$ in the GHH model.8

These values of the innovation standard deviation are close to the values used by BCF, Danthine and Donaldson (2002), and Storesletten, Telmer, and Yaron (2007) in a context similar to ours. Nevertheless, these figures are quite high compared to the direct estimate of the volatility of Solow residuals for the postwar period, which is about 0.7%. This suggests that it may be more appropriate to interpret the exogenous driving source in this class of models as encompassing more than just technology shocks (such as fiscal policy shocks, among others).

^aThe Sharpe ratio of 0.25 is one of the two empirical targets in the calibration. All statistics are reported in annualized percentages. Annual returns are calculated by summing log monthly returns. The numbers in parentheses in the second column are the standard errors of the statistics to reflect the sampling variability in the U.S. data.

^bThe value reported here represents an approximate lower bound for this ratio based on the empirical evidence discussed in Section 5.1.

⁸These volatility figures are helped a bit by the choice of a monthly decision frequency and time aggregation of the resulting simulated data. If, instead, the model were solved at quarterly frequency, the values of σ_{ε} necessary to match the same targets would be 10%-15% higher, depending on specification.

 $^{^9}$ BCF used permanent shocks with $\sigma_{\varepsilon} = 1.8\%$ per quarter; Storesletten, Telmer, and Yaron (2007) also used permanent shocks with $\sigma_{\varepsilon} = 3.3\%$ per year. Danthine and Donaldson (2002) used a two-state Markov process with persistence of 0.97 and a $\sigma_{\varepsilon} = 5.6\%$ per quarter.

4. MODEL RESULTS: ASSET PRICES

4.1. The Unconditional Moments of Asset Prices

I begin by discussing the unconditional moments of stock and bond returns, and then turn to the conditional moments in the next section. Table II displays the statistics from the simulated CONS model along with their empirical counterparts computed from the historical U.S. data covering the period 1890–1991. I first examine the inelastic labor supply case. This case provides a useful benchmark, both because it is the most common case studied in the literature and because it allows one to understand the key mechanisms generated by limited participation without the added complexity of labor supply choice.

The Equity Premium

As shown in the third column of Table II, in the calibrated model the target Sharpe ratio of 0.25 is attained with a moderately high risk aversion of 6. Clearly, a given Sharpe ratio can be generated by many different combinations of equity premium and volatility, so matching this target does not say anything about the numerator and the denominator. The corresponding equity premium is 5.45%, which is slightly lower than the historical figure of 6.2%. The volatility of the equity premium is 21.9% compared to 19.4% in the data. Therefore, the model generates an equity premium with mean and volatility that are in the right ballpark compared to the data.

The Mechanism

The high equity premium is generated by a general equilibrium mechanism that amplifies stockholders' consumption growth volatility and does so in a procyclical fashion, causing them to demand a high equity premium. Specifically, the mechanism results from the interaction of three features of the model, which reinforce each other. First, limited participation creates an asymmetry in consumption smoothing opportunities: facing persistent (aggregate) labor income shocks, non-stockholders have to exclusively rely on the bond market, whereas stockholders have another margin—they can also adjust their capital holdings. Second, because of their low EIS, non-stockholders have a stronger desire for a smooth consumption process compared to stockholders. The combination of these two effects implies that non-stockholders need the bond market much more than stockholders. Third, and importantly, the bond market is not a very effective device for consumption smoothing in the face of aggregate

¹⁰The data are taken from Campbell (1999). The stock return and the risk-free rate are calculated from Standard and Poor's 500 index and the 6-month commercial paper rate (bought in January and rolled over in July), respectively. All returns are real and are obtained by deflating nominal returns with the consumption deflator series available in the same data set.

risk, because it merely reallocates the risk rather than reducing it, as would be the case if shocks were idiosyncratic. As a result, non-stockholders' desire for smooth consumption is satisfied via trade in the bond market, at the expense of higher volatility in stockholders' consumption. Moreover, since these large fluctuations in stockholders' consumption are procyclical, they are reluctant to own the shares of the aggregate firm that performs well in booms and poorly in recessions. Therefore, they demand a high equity premium. In Section 5, I quantify the role of this mechanism and contrast it with earlier models of limited participation, such as Saito (1995) and Basak and Cuoco (1998).

The Risk-Free Rate

Turning to the risk-free rate, the mean is 1.3%, which compares well to the low average interest rate of 1.9% in the data. It is important to note that the low risk-free rate is helped by the fact that the model abstracts from long-run growth *and* preferences are of the Epstein–Zin form. To see this, consider the following expression for the *log* risk-free rate, which holds as a fairly good approximation:¹¹

(9)
$$r_t^f \approx -\ln \beta + \rho^h E_t(\Delta \log c_{t+1}^h) + \kappa,$$

where κ contains terms that involve the volatility of consumption and wealth, which turns out to be secondary for the present discussion.

With secular growth, the consumption growth term on the right-hand side would be nonzero—unlike in the present model—pushing the average risk-free rate up. For example, taking an annual growth rate of 1.5%, and setting $\rho^h=3.33$ as calibrated above would imply $r_t^f=5.85\%$. As is well known, this "risk-free rate puzzle" is even more severe with CRRA utility, because in this case it would be the risk aversion parameter that would appear in front of the second term, which is $\alpha^h=6$ in this case, implying $r_t^f=10.2\%$. This discussion reiterates the well-known point that models with CRRA utility functions and long-run growth that match the equity premium typically imply a high average interest rate. Epstein–Zin preferences mitigate this problem if one assumes an EIS that is higher than the reciprocal of the risk aversion parameter, as is the case here.

Another well-documented feature of the interest rate—and as it turns out, a challenging one to explain—is its low volatility. The standard deviation is 5.44% in the historical sample, although different time periods (such as the postwar sample) can yield values as low as 2% per year (see, e.g., Campbell (1999) for a discussion). The corresponding figure is 6.65% in the model (and

¹¹For an exact derivation of this expression, human wealth would need to be tradeable. Although this is not the case in the present model, the equation holds fairly well and provides a useful approximation.

TABLE III
UNCONDITIONAL MOMENTS OF ASSET RETURNS: MODEL WITH ELASTIC LABOR SUPPLY

	U.S. Data	Model			BCF	D-D
Endogenous Leisure?		CD	$GHH_{Baseline}$	GHH _(Low Frisch)	Linear	None
	A	. Stock ar	nd Bond Return	ns		
$E(R^{\mathrm{ep}})$	6.17 (1.99)	2.65	4.21	4.03	6.63	5.23
$\sigma(R^{\mathrm{ep}})$	19.4 (1.41)	15.4	17.4	18.1		25.3
$\sigma(R^s)$	18.7 (1.38)	14.8	16.5	17.9	18.4	24.3
$E(R^{\rm ep})/\sigma(R^{\rm ep})$	0.32(0.11)	0.17	0.24	0.22	0.36^{a}	0.21
$E(R^f)$	1.94 (0.54)	2.87	1.42	1.73	1.20	1.32
$\sigma(R^f)$	5.44 (0.62)	4.91	4.10	4.46	24.6	10.61
		B. Price-	Dividend Ratio)		
$E(P^s/D)$	22.1 (0.58)	25.7	24.7	25.9	_	_
$\sigma(\log(P^s/D))$	26.3 (1.67)	13.6	17.8	19.1	_	_
$\sigma(\Delta \log D)$	13.4 (0.94)	14.8	11.2	11.9	_	4.55

^aBCF reported the time average of the conditional Sharpe ratio, $E_t(R^{\rm ep})/\sigma_t(R^S)$, instead of the unconditional Sharpe ratio reported in the present paper. The statistics from BCF refer to their benchmark model (called the preferred two sector model), which has the best overall performance. The statistics from Danthine and Donaldson (2002, D-D) are from their Table 6, right column with smoothed dividends, which generates the best overall performance. A dash indicates that the corresponding statistic has not been reported in that paper. In the fifth column, the Frisch elasticity is set to 0.5 and the σ_E is recalibrated to 1.3% per quarter to match output volatility.

further falls to 4.1% with endogenous labor supply below). Although this figure is higher than the empirical values, the low volatility of the interest rate has turned out to be quite difficult to generate, especially in macro-based asset pricing models. For example, as I report in Table III, this volatility is 24.6% in BCF and 10.6% in Danthine and Donaldson (2002); it is 11.5% in Jermann (1998) (not reported). Thus, the present model provides a step in the right direction. So what explains the relatively low variability of interest rates in the model?

To understand the mechanism, consider the bond market diagram in Figure 1. The left panel depicts the case of a representative agent with a low EIS, which is a feature common to the models mentioned above. For example, both the endogenous and the external habit models imply a low EIS (despite differing in their risk aversion implications). With a low EIS, however, the interaction of the resulting inelastic (steep) bond demand curve with a bond supply that is *perfectly inelastic* at zero (because of the representative–agent assumption) means that even small shifts in the demand curve—due to labor income shocks and the consequent change in the demand for savings—generate large movements in the bond price and, hence, in the risk-free rate.

In the present model, the mechanism is different. First, for the following discussion it is convenient to label non-stockholders' bond decision rule as the "bond demand" and the negative of stockholders' bond decision rule as the "bond supply." Now notice that the majority—80%—of the population (non-

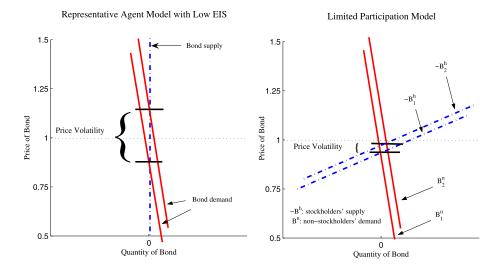


FIGURE 1.—Determination of bond price volatility.

stockholders) have a very low EIS as before, implying very inelastic bond demand (right panel). Turning to bond supply, the key difference here is that it is not inelastic at all. In fact, the stockholders' supply curve is rather flat, both because of their higher EIS and because they have another asset—equity in the firm—that can act as a partial substitute for bond. As a result, a shift in the bond demand curve (resulting from fluctuations in non-stockholders' labor income) of similar magnitude as before now results in smaller fluctuations in the interest rate, and the rest is reflected in the variability of trade volume.

The Price-Dividend Ratio

The average price-dividend (P/D) ratio in the CONS model is 27.2, which is about 20% higher than the average of 22.1 in the data. Its volatility is 26.6%, which compares fairly well with the empirical figure (26.2%). Finally, the volatility of dividend growth is 19.1%, which is too volatile compared to the 13.4% figure in the U.S. data. This high volatility is due to the leverage in the capital structure and is one of the dimensions with which the labor supply choice will help.

4.2. The Role of Preference Heterogeneity

One advantage of Epstein–Zin utility is that it allows me to easily examine the effects of heterogeneity in the EIS and risk aversion parameters on asset prices. I conduct three experiments reported in the last three columns of Table II. First (fourth column), I keep all aspects of the baseline parametrization intact, but only *increase* non-stockholders' EIS from 0.1 to 0.3, which eliminates

all preference heterogeneity from the model. With this change, the equity premium falls significantly, from 5.5% to 2.44%, and its volatility falls from 21.9% to 15.3%. More importantly, the price of risk falls from 0.25 to 0.16. Moving down the column, the volatilities of all variables go down—by 30%–50%. This makes some variables, such as the P/D ratio, too smooth compared to the data, while bringing some others closer to their empirical counterparts, such as the interest rate and dividend growth volatilities. Overall, these results show that the EIS of non-stockholders has a major impact on asset prices, perhaps most importantly on the equity premium and the Sharpe ratio, which are key statistics that this model seeks to explain.

Second, an alternative way to eliminate preference heterogeneity is by *reducing* the EIS of stockholders from 0.3 to 0.1, which, as could be anticipated, has qualitatively the opposite effect (fifth column). The equity premium now increases to 7.65%, but the volatility is also higher at 27.2%. As a result, the rise in the Sharpe ratio remains rather modest: it is 0.28, up from 0.25. Finally, other volatilities—that of the interest rate, P/D ratio, and dividend growth—are also significantly higher. Therefore, stockholders' EIS has a larger effect on volatilities, but a smaller effect on the Sharpe ratio.

The two experiments above also reveal another role played by the EIS heterogeneity. As mentioned earlier, in the U.S. data, stockholders' consumption growth is more volatile than non-stockholders': $\sigma(\Delta \log c^h)/\sigma(\Delta \log c^n) > 1.5 - 2.0$ (see Section 5.1 for more details). The baseline CONS model is consistent with this empirical fact, generating a ratio of volatilities equal to 2.42 (panel C of Table II). However, if preference heterogeneity is eliminated, this ratio falls from 2.42 to 0.78 in the fourth column and to 1.12 in the fifth column. This is because stockholders have access to two separate assets that they can use to smooth consumption effectively and, absent preference heterogeneity they choose to do exactly that. (Notice that this result also explains why reducing stockholders' EIS in the fifth in column above had a small effect on the Sharpe ratio.)

To summarize the findings so far, the low EIS of non-stockholders plays an important role in generating a high Sharpe ratio, whereas lowering stockholders' EIS has a larger effect on asset price volatilities, but only a small effect on the Sharpe ratio; furthermore, it creates a counterfactually low consumption growth volatility for this group. The baseline calibration—with EIS heterogeneity—generates results consistent with both asset prices *and* the relative consumption volatility of the two groups.

Third, and finally, in the last column, I examine the effect of non-stockholders' risk aversion by doubling it to 12. Comparing the sixth column to the baseline case in the third column shows that this change has a minor effect, if at all, across the board. Surprisingly, doubling the risk aversion of 80% of the population has very little impact on the unconditional moments of asset prices. Loosely speaking, this is due to the fact that non-stockholders' only direct effect on asset prices is through the bond market and their (precautionary) bond

demand is largely determined by their EIS, but very little influenced by their risk aversion.¹²

4.3. Asset Prices With Endogenous Labor Supply

In the previous section, I found that the benchmark model with inelastic labor supply generated plausible behavior for the unconditional moments of stock and short-term bond returns. Nevertheless, labor supply choice is central for any serious macroeconomic analysis. Therefore, I now relax the inelastic labor supply assumption and consider the two utility functions—Cobb–Douglas and GHH—described above.

Results

Table III reports the results (third to fifth columns). To provide a comparison, the last two columns display the same set of statistics from two leading macro-based asset pricing models proposed in the existing literature, namely BCF and Danthine and Donaldson (D-D) (2002). The first paper features an endogenous labor–leisure choice, whereas the latter paper has inelastic labor and is more comparable to the model analyzed in the previous section.

With Cobb–Douglas utility (CD model, third column), the first point to observe is the rather large fall in the equity premium, which is now 2.65% (compared to 5.5% with inelastic labor supply), accompanied by a smaller fall in the volatility (which is 15.4% compared to 21.9% before), resulting in a fall in the Sharpe ratio from 0.25 to 0.17. Moving down the column, notice that both the risk-free rate and the dividend growth are less volatile than before and now are closer to their respective empirical values. The P/D ratio is also less volatile and is now too smooth compared to data. Overall, I view these results as a step backward compared to the model with inelastic labor supply.

I next turn to the GHH model in the fourth column, which delivers a more respectable equity premium level of 4.2%, with a volatility of 17.5%. The resulting Sharpe ratio is 0.24, slightly lower than in the model with inelastic labor supply. Furthermore, the volatility of the risk-free rate is 4.1%, which is lower than the model with inelastic labor supply (at 6.65%). As noted earlier, this low volatility is also an important improvement of this model over earlier production economy models. As for the price—dividend ratio, the volatility is about 70% that in the data, but higher than in the model with CD preferences. The volatility of dividend growth now falls to 11.2% annually. Overall, the model with GHH preferences displays asset pricing behavior that is comparable to the model with inelastic labor supply.

In the next column, I explore the impact of lowering the Frisch elasticity closer to the values reported in the microeconomics literature. I set $1/\gamma$ to 0.5

¹²Furthermore, in the supplementary appendix, I also report the results on asset price dynamics for $\alpha^n = 12$ and find that they are very similar to the case with $\alpha^n = 6$.

following Domeij and Floden (2006), who surveyed existing microeconometric studies and argued that part of the reason for the very low estimates is the bias that arises from ignoring borrowing constraints. This change in calibration has a relatively modest effect on statistics: most notably, the equity premium falls slightly to 4% and the Sharpe ratio falls to 0.22. As I discuss in Section 6.1, the main drawback of this calibration is that it implies a labor hours process that is too smooth, which is also why macroeconomists typically use higher values similar to those in the baseline calibration.

It is useful to compare these results to earlier studies. In the working paper version, BCF showed that introducing a flexible labor supply choice reduces the equity premium substantially, from 4.45% to 0.15%, and reduces the Sharpe ratio from 0.27 to 0.03. 13 One goal of their paper, then, is to identify some prominent labor market frictions that overcome this difficulty associated with endogenous labor supply. Their baseline model features such a framework that matches the historical equity premium as well as a number of other unconditional moments (reported in the sixth column of Table III).

In comparison, here flexible labor supply choice has a smaller negative impact on the Sharpe ratio, especially with GHH preferences. This difference stems from two sources. First, BCF employed a specification where utility is linear in leisure and separable from consumption. Consequently, fluctuations in labor hours have no direct effect on utility, which makes it relatively costless to smooth consumption fluctuations by adjusting one's labor supply. The only loss comes from the fact that to smooth fluctuations, labor supply would need to move in the opposite direction dictated by the substitution effect: rise in recessions when wages are low and fall in expansions when wages are high. In contrast, with the nonseparable preferences in this paper, agents do care about fluctuations in leisure as well as how leisure comoves with consumption, which makes it more costly to adjust labor supply to suppress fluctuations in the marginal utility of consumption. Second, with GHH preferences there is no wealth effect on labor supply choice, so labor hours are strongly procyclical due to the substitution effect of wages over the business cycle, making it an even less effective tool for smoothing fluctuations in marginal utility. As a result, the price of risk does not fall as much in this framework when labor supply choice is endogenized.

4.4. The Dynamics of Asset Prices

I now examine the extent to which the limited participation model captures some salient aspects of asset price dynamics. As mentioned earlier, some of these features, such as the countercyclical price of risk, have been difficult to generate in some asset pricing models. The results reported below are from

¹³See Boldrin, Christiano, and Fisher (1999, Table II). The statement in the text is based on comparing the results in column 4 to column 8.

the GHH model, but I found these statistics to be remarkably robust across the different specifications analyzed in this paper.¹⁴

4.4.1. Mean Reversion and Predictability of Returns

I begin with the price—dividend ratio, which is procyclical in the model, consistent with empirical evidence, with a correlation of 0.73 with output. The procyclicality follows from the fact that when the persistent technology shock hits the economy, the stock price capitalizes all future productivity gains upon impact and thus increases substantially, while the initial response of dividends is muted due to the gradual rise of the capital stock after the shock (because of adjustment costs), making the ratio of the two variables procyclical.

A second well-known observation concerning the equity premium is that it tends to revert to its mean over time. The first row of Table IV displays the autocorrelations of the equity premium from the U.S. data. Notice that these autocorrelations are close to zero, which makes it difficult to measure them precisely. As a result, they are not uniformly negative. To circumvent this problem, an alternative statistic used in the literature aggregates consecutive autocorrelation coefficients, which reveals a stronger pattern of mean reversion (third row). The second and fourth rows display the model counterparts of the two measures of mean reversion, which are consistent with the signs and rough magnitudes of these statistics in the data.

The finding of mean reversion is a clear departure from the martingale hypothesis of returns and is closely linked to the predictability of returns documented by Campbell and Shiller (1988), among others. To show this, I first regress log stock returns on the log price-dividend ratio using the historical

TABLE IV	
THE AUTOCORRELATION STRUCTURE OF KEY FINANCIAL VAI	RIABLESa

		Autocorrelation at Lag j (years)				
	1	2	3	5	7	
$ \begin{array}{c} r^s - r^f \\ \text{U.S. data} \\ \text{Model} \end{array} $	0.03 -0.03	-0.22 -0.03	$0.08 \\ -0.02$	-0.14 -0.02	0.10 -0.02	
$ \sum_{i=1}^{j} \rho[(r^s - r^f)_t, (r^s - r^f)_{t-i}] $ U.S. data Model	$0.03 \\ -0.03$	-0.19 -0.06	-0.11 -0.08	-0.29 -0.13	-0.15 -0.15	

^aStatistics from the model are calculated from annualized values of each variable, except for the stock price, which is taken to be the value at the end of the year.

¹⁴The supplementary appendix reports the counterparts of the tables in this section for the CONS and CD models.

	U.S. Da	ta	Model	
Horizon (k)	Coefficient	R^2	Coefficient	R^2
	A. Sto	ock Returns		
1	-0.21	0.07	-0.19	0.09
2	-0.36	0.12	-0.40	0.16
3	-0.41	0.13	-0.49	0.22
5	-0.70	0.23	-0.77	0.28
7	-0.87	0.27	-0.91	0.35
	B. Exc	cess Returns	3	
1	-0.22	0.09	-0.11	0.02
2	-0.39	0.14	-0.20	0.04
3	-0.47	0.15	-0.29	0.06
5	-0.77	0.26	-0.42	0.10
7	-0.94	0.33	-0.49	0.12

TABLE V
LONG-HORIZON REGRESSIONS ON PRICE–DIVIDEND RATIO^a

U.S. data (panel A of Table V). The well-known pattern documented in the literature can been seen here: the coefficients are negative, indicating that a high price–dividend ratio forecasts lower returns in the future. Moreover, both the coefficients and the R^2 values are increasing with horizon. The model counterpart is reported in the last two columns. The coefficient estimates and the R^2 's are consistent with empirical results: predictability is modest at the 1-year horizon, but increases steadily, reaching 35% at the 7-year horizon. The coefficients also increase quickly first and then grow more slowly. Overall, the model generates significant predictability of stock returns.

Turning to excess returns in panel B of Table V, the predictability in the U.S. data is evident again. The last two columns report the same regressions using simulated data. The coefficients on the price-dividend ratio are negative and increase in absolute value with horizon consistent with the data. However, the amount of predictability is smaller than in the data: the R^2 of the regression is only 12% at the 7-year horizon compared to 33% in the data. Thus, the model is qualitatively consistent with excess return predictability, but does not quantitatively capture the total magnitude observed in the U.S. data.

4.4.2. Countercyclical Variation in the Price of Risk

I now examine the cyclical behavior of the conditional moments. Figure 2 plots the typical simulated paths of the expected equity premium and Sharpe

^aThe table reports the coefficients and R^2 values of the regression of log stock returns (top panel) and log excess returns (bottom panel) on the log price-dividend ratio. Horizon (k) is in years.

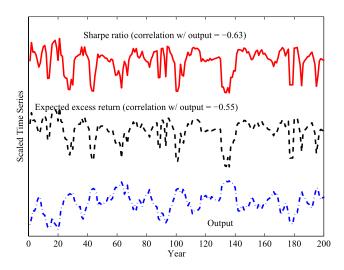


FIGURE 2.—The cyclical behavior of expected excess returns and the Sharpe ratio.

ratio against output over a period of 200 years. ¹⁵ Consistent with the U.S. data (Chou, Engle, and Kane (1992)), both the expected premium and the Sharpe ratio rise visibly in recessions and fall in expansions (correlation with output is -0.55 and -0.63, respectively). Moreover, the conditional volatility is also countercyclical and has a correlation with output of -0.42 (to save space, the plot is not included in the figure). The conditional moments are also quite variable: the 95% confidence interval for the expected excess return extends from 1.3% to 4.8%, and the 95% confidence interval for its conditional volatility extends from 9.1% to 18.5%. The fact that expected returns are more variable than conditional volatility (as measured by their coefficient of variation) results in the countercyclicality of the Sharpe ratio mentioned above. With few exceptions, ¹⁶ this countercyclicality of the market price of risk has been difficult to generate in consumption-based asset pricing models. In the next section, I explain the new mechanism in this model which generates this result.

5. UNDERSTANDING THE SOURCES OF EQUITY PREMIUM

The large and countercyclical equity premium arises from the interaction of (i) limited stock market participation, (ii) the low EIS of non-stockholders, and (iii) consumption smoothing in the face of persistent (aggregate) labor income shocks. What distinguishes the mechanism in this paper from earlier

¹⁵Each series is rescaled by its standard deviation and shifted vertically to fit in the same graph. Thus, while the amplitudes are not informative, the comovement between the series is preserved. ¹⁶Most notably, Campbell and Cochrane (1999) and Bansal and Yaron (2004).

models of limited participation is (ii) and (iii). These two features combine to make the *timing* of trade in the bond market the driving force behind the high equity premium. In this section I quantify this mechanism. Because labor supply choice adds another level of complexity to the analysis, in this section, I focus on the CONS model.

5.1. Why Is There a High Equity Premium?

The annual standard deviation of consumption growth in the CONS model is 3.61% for stockholders, but only 1.48% for non-stockholders. To quantify the sources of stockholders' consumption volatility, I first substitute the equilibrium conditions (iii)(a) and (b) (from the end of Section 2) as well as the expression for dividends into the budget constraint of a stockholder, and after some straightforward manipulation, I obtain

(10)
$$c^{h} = \underbrace{\left(W + \frac{\theta Z K^{\theta} L^{1-\theta} - I}{\mu}\right)}_{A^{h}} - \underbrace{\frac{(B - P^{f} B')}{\mu}}_{g^{h}}.$$

This expression provides a useful decomposition. Part of the variation in stockholders' consumption comes from aggregate sources, that is, fluctuations in wage and capital income, which is denoted by A^h . The scaling factor $1/\mu$ that appears in A^h reflects the fact that aggregate capital income risk is concentrated among stockholders, since they are the sole capital owners in this economy. However, this risk only has a modest contribution to the volatility of their consumption, as will become clear shortly. A second part of variability arises from trade with the non-stockholders in the bond market: the component denoted by $a^h \equiv (B - P^f B')/\mu$ measures the *net interest payments* received by non-stockholders, which is made by stockholders indirectly through the firm they own. Using equation (10), stockholders' consumption growth volatility can be approximated as

(11)
$$\operatorname{var}(\Delta \log c^h) \approx \operatorname{var}(\Delta \log A^h) + \operatorname{var}\left(\Delta \frac{a^h}{A^h}\right) + 2\operatorname{cov}\left(\Delta \log A^h, -\Delta \frac{a^h}{A^h}\right).$$

Similarly, non-stockholders' consumption can be written as $c^n = W + (B - P^f B')/(1 - \mu)$, and the variance of their consumption growth is obtained by replacing A^h and a^h in equation (11) with $A^n \equiv W$ and $a^n \equiv -a^h \mu/(1 - \mu)$, respectively.

The top panel of Table VI shows that interest payments are very small on average, making up a small fraction of consumption: $E(a^i)/E(c^i)$ is less than

TABLE VI
DECOMPOSITION OF CONSUMPTION VOLATILITY AND EQUITY PREMIUM ^a

		Fraction of $E(c^i)$ Explained by			
		$E(A^i)/E(c^i)$	$E(a^i)/E(c^i)$		
Stockholders		1.011	0.011		
Non-stockholders		0.995	0.005		
		Fraction of σ^2	$\Delta \log c^i$) Accounte	ed for by	
	$\sigma^2(\Delta \log c^i)$	$\sigma^2(\Delta \log A^i)$	$\sigma^2(\Delta \frac{a^i}{A^i})$	$2\sigma(\Delta \log A^i, -\Delta \frac{a^i}{A^i})$	
Stockholders	$(3.61\%)^2$	0.185	0.340	0.475	
Non-stockholders	$(1.48\%)^2$	3.13	0.61	-2.74	

 $a_i = h, n$. See the text and equation (10) for the definitions of a^i and A^i .

1.01% for both stockholders and non-stockholders. However, interest payments are volatile and, more importantly, they vary systematically with the business cycle. This is shown in the lower panel of Table VI, which displays the fraction of consumption growth variance explained by each of the three terms in equation (11). For stockholders, only 18.5% of consumption growth variance is attributable to fluctuations in aggregate income, despite the fact that this component makes up nearly all of their average consumption (row 1). Hence, the concentration of aggregate *capital* income risk, included in A^h , contributes only modestly to consumption fluctuations and, consequently, to the equity premium. The main source of volatility for stockholders comes from the bond market: interest payments, a^h , account for the remaining three-quarters of variance (0.34 + 0.475). What is really crucial for this extra volatility is the timing of interest payments: $\operatorname{corr}(\Delta \log A^h, \Delta(a^h/A^h)) = -0.947$ (which can be calculated from the third row of Table VI), which means that the payments received by the non-stockholders increase exactly when aggregate income falls, that is, in recessions. 17 Therefore, consumption smoothing for nonstockholders comes at the expense of large fluctuations in stockholders' consumption, so the covariance term in the third column accounts for nearly half of the total volatility. The flip side of this story is seen in the variance of nonstockholders: $var(\Delta \log c^n)$ would be 3.13 times higher were it not for the consumption smoothing provided by stockholders through the bond market (that is, if the bond market were shut down, so $a_t^h \equiv 0$).

¹⁷This negative correlation is not due to the appearance of A^h in the first term as well as in the denominator of the second term. To verify this, I also calculated $\operatorname{corr}(\Delta \log A^h, \Delta a^h) = -0.953$, which is as negative as the reported correlation.

A Comparison to Earlier Models

The mechanism proposed in this paper differs from earlier models with limited participation in two key dimensions. First, in Saito (1995) and Basak and Cuoco (1998), non-stockholders begin life with some financial wealth but do not have a labor income flow. The only way to sustain consumption is then by investing this wealth in the bond market. As a result, each period nonstockholders receive substantial interest payments from stockholders, which in turn leverages the capital income of the latter group and amplifies their consumption volatility. Although this is a potentially powerful mechanism, for it to work, interest payments need to be substantial—as large as the consumption of non-stockholders—which in turn implies that non-stockholders must hold a large fraction of aggregate wealth. This counterfactual implication has been one of the main criticisms raised against these models. In contrast, as noted above, the interest payments in the present model are very small, and, as we shall see below, the fraction of aggregate wealth held by non-stockholders is also small and consistent with empirical evidence. Instead, the amplification here is generated by the cyclical nature of these payments that serve to insure non-stockholders against aggregate fluctuations.

The mechanism in Danthine and Donaldson (2002) is more closely related to the present paper. In their model, entrepreneurs smooth fluctuations in their workers' consumption at the expense of extra volatility in their own consumption, which results in a high equity premium. An important difference from the present model is that this smoothing happens through insurance within the firm, instead of being through the bond market. As a result, the bond price is determined by the entrepreneurs alone (and not jointly with workers, which is the case here). It would be interesting to know if this difference would result in different implications for asset price dynamics, which is not explored in that paper.

A second difference from previous models is that here preference heterogeneity is essential for amplifying stockholders' consumption volatility relative to that of non-stockholders. This point has already been discussed in Section 4.2, so I do not repeat it here, but it is important to note that this feature contrasts with the previous papers mentioned above, where non-stockholders have no choice but to lend to stockholders simply to survive, which amplifies the consumption volatility of the latter group regardless of preference heterogeneity.

Empirical Evidence

Finally, the high volatility of stockholders' consumption relative to that of non-stockholders is well documented empirically. For example, Mankiw and Zeldes (1991) found the ratio of standard deviations to be 1.6 using the Panel Study of Income Dynamics data, although their consumption measure consists of only food expenditures, which is likely to understate the true volatility ratio for nondurables. Attanasio, Banks, and Tanner (2002) used expenditures

on nondurables and services from the U.K. Family Expenditure Survey and calculated stockholders' volatility to be 1.5 to 2 times larger than that of non-stockholders. Another piece of evidence comes from Aït-Sahalia, Parker, and Yogo (2004), who documented that the sales of luxury goods (such as expensive French wine, charitable donations, rents on luxury condos in Manhattan, etc.) display volatility that exceeds the standard deviation of aggregate nondurables consumption by a factor of 5–10. They interpreted this finding as indicative of highly volatile expenditures by the very wealthy.

5.2. Why Is the Equity Premium Countercyclical?

It is instructive to start from the following decomposition of the *conditional* Sharpe ratio that can be derived under CRRA preferences. ¹⁹ Although I use recursive utility in the present model, it turns out that the same decomposition still holds fairly well here and is useful for understanding the source of time variation: ²⁰

(12)
$$SR_t \equiv \frac{E_t(R_{t+1}^{ep})}{\sigma_t(R_{t+1}^{ep})} \approx \alpha^h \times \sigma_t(\Delta \log c_{t+1}^h) \times corr_t(\Delta \log c_{t+1}^h, R_{t+1}^{ep}).$$

The conditional correlation term in (12) is close to 1 and is very stable over the business cycle, and α^h is simply a constant. Therefore, equation (12) points to $\sigma_t(\Delta \log c_{t+1}^h)$ as the source of time variation in the Sharpe ratio. Indeed, in the model, SR_t is 48% higher during a recession than it is in a boom, and $\sigma_t(\Delta \log c_{t+1}^h)$ is 39% higher in a recession than in a boom, explaining a large fraction of the countercyclicality in SR_t . Moreover, because conditional volatility, $\sigma_t(R_{t+1}^{ep})$, is also countercyclical (18% higher during recessions) the

¹⁸These figures are likely to be downward biased because existing measures of stockholders' consumption are based on micro data sets that contain few "extremely rich" households, that is, those in the top 1% of the wealth distribution. At the same time, these households own nearly *half* of all stocks, and the top 0.5% own 37% of all stocks (Poterba and Samwick (1995)).

¹⁹Two additional assumptions that are needed to derive the decomposition are that portfolio constraints are not binding, and consumption growth and asset returns are homoskedastic and jointly log-normal.

²⁰Although one can also derive an exact decomposition of the Sharpe ratio with recursive preferences (Campbell (1999, eq. 22)), I do not use this alternative form because (i) it requires the additional assumption of complete markets (or human wealth to be tradeable) and (ii) the decomposition has the same form as the one used here, but adds a second term that involves the covariance of the equity premium with the return on wealth. The contribution of this second term depends on the values of risk aversion and EIS, and, for the values used in this paper, it does not seem to be of first order importance for the cyclical behavior. Therefore, I opt for the simpler decomposition, which is useful for discussing the mechanism.

 21 A recession is defined as the states of the world when output is 1 standard deviation or more below the mean, that is, $Y_t < E(Y) - \sigma(Y)$. An expansion is defined analogously: $Y_t > E(Y) + \sigma(Y)$. Using average output as the dividing line, I get $E[\sigma_t(\Delta c_{t+1}^h)|Y_t < E(Y)]/E[\sigma_t(\Delta c_{t+1}^h)|Y_t > E(Y)] = 1.23$.

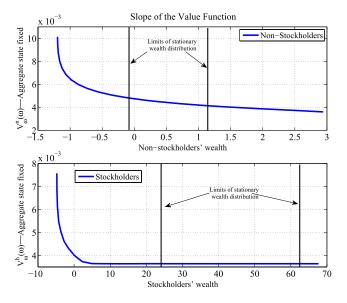


FIGURE 3.—Change in the slope of value functions with wealth level.

expected equity premium, $E_t(R_{t+1}^{ep})$, is 68% higher during recessions compared to booms.

The natural question that follows is, "Why is the stockholders' consumption growth volatility countercyclical?" To answer this question, two points should be noted. First, a well-known feature of the consumption–savings problem in the presence of uninsurable income risk is that the value function has more curvature at lower wealth levels and less curvature at higher wealth levels. While this is well known in the expected utility case, the same is true here with recursive preferences, as can be seen from Figure 3, which plots how the slopes of V^h and V^n change with ω (keeping aggregate state variables fixed). If markets were complete, with the formulation of recursive preferences in (1), the value functions would be linear in wealth (Epstein (1988)), implying that the slopes would be *constant* in wealth. This is obviously not the case for either agent in Figure 3, owing to incomplete markets.

Moreover, and thus second, non-stockholders own substantially less wealth per capita than stockholders (more on this in Section 6.3). Figure 3 shows the bounds of the ergodic distribution of wealth for each type of agent, where this difference in wealth levels is evident. Thus, non-stockholders are on the part of their value function that has high curvature: a relatively small change in their wealth holdings changes their attitudes toward risk and, consequently, changes their precautionary savings demand significantly. This is clearly not the case for stockholders, who remain on the very flat part of their value function over the business cycle. To further illustrate this point, Figure 4 plots the normalized curvature of the value function (i.e., risk aversion with respect to

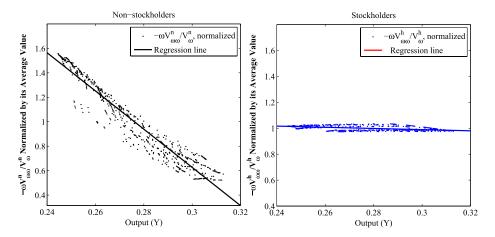


FIGURE 4.—Change in attitudes toward risk over the business cycle.

wealth gambles), $-\omega V_{\omega\omega}^i/V_{\omega}^i$, for each type of agent as a function of realized output using simulated data from the CONS model. I normalize the average value to 1 for both groups so that the vertical axis can be interpreted as the *percentage change* in risk attitudes over the business cycle. The effect described above can be clearly seen here: non-stockholders' risk aversion increases significantly in recessions (and consequently, their demand for insurance), whereas it barely moves for stockholders. Combining this countercyclical change in non-stockholders' demand for consumption smoothing with the mechanism described in the previous section implies that there should be more trade in the risk-free asset market in recessions. This is exactly what happens: $\rho(|a_t^h|, Y_t) = -0.55$, which shows that the average size of interest payments increases—in turn raising stockholders' consumption growth volatility—during recessions.²³

Finally, in contrast to the 39% rise in $\sigma_t(\Delta \log c_{t+1}^h)$ mentioned above, $\sigma_t(\Delta \log c_{t+1}^n)$ goes down slightly—by 10%—in recessions. Of course, this is entirely consistent with the mechanism discussed above whereby non-stockholders have an even stronger desire for a smooth consumption process during recessions. Nevertheless, because the two groups' conditional volatili-

 $^{^{22}} Risk$ aversion with respect to wealth gambles depends on the market structure in addition to α .

²³Notice that the countercyclicality of trade volume reflects larger transfers of *both signs* in the bond market during recessions. This can be seen more clearly by calculating $E(a_t^h|\text{recession}, \Delta Y_t < 0) = 0.62 > 0.40 = E(a_t^h|\text{boom}, \Delta Y_t < 0)$ and $E(a_t^h|\text{recession}, \Delta Y_t > 0) = -0.66 < -0.43 = E(a_t^h|\text{boom}, \Delta Y_t > 0)$. Thus, because non-stockholders are more averse to fluctuations during recessions, they borrow more aggressively when they receive a negative shock to prevent an *immediate fall* in consumption; when they receive a positive shock, they save more aggressively as a buffer stock to self-insure against *future* negative shocks.

ties move in opposite directions over the business cycle, aggregate consumption growth volatility exhibits little time variation (goes up by only 8% in recessions), masking the large cyclical changes in $\sigma_t(\Delta \log c_{t+1}^h)$ responsible for the countercyclical Sharpe ratio. A corollary to this observation is that if a researcher studies equation (12) with the aggregate consumption process (as would be the case in a representative agent framework), the lack of time variation in the volatility of aggregate consumption growth would lead the researcher to require the curvature parameter, α , to be time-varying so as to explain the countercyclicality of SR_t . This is the approach adopted, for example, in Campbell and Cochrane (1999), among others.

6. MODEL RESULTS: MACROECONOMIC QUANTITIES

In this section I examine the implications of the model for macroeconomic quantities along two dimensions. I first analyze the performance of the model for business cycle statistics and then turn to the cross-sectional implications.

6.1. Business-Cycle Implications

Table VII displays standard business cycle statistics from the U.S. data as well as their counterparts from the CD and GHH models. As before, the last two columns report the corresponding figures from BCF and Danthine and Donaldson (2002) for comparison.

TABLE VII	
BUSINESS CYCLE STATISTICS IN THE LLS	DATA AND IN THE MODEL a

	Data	Model			BCF	D-D
Leisure Preferences		CD	GHH _{Baseline}	GHH _{Low Frisch}	Linear	None
			Volati	ility		
$\sigma(Y)$	1.89 (0.21)	1.97	1.95	1.96	1.97	1.77
$\sigma(C)/\sigma(Y)$	0.40(0.04)	0.92	0.78	0.75	0.69	0.82
$\sigma(I)/\sigma(Y)$	2.39 (0.06)	1.38	1.76	1.86	1.67	1.72
$\sigma(L)/\sigma(Y)$	0.80 (0.05)	0.07	0.50	0.32	0.51	_
			Correlation V	Vith Output		
$\rho(Y,C)$	0.76(0.05)	0.99	0.99	0.99	0.95	0.96
$\rho(Y,I)$	0.96 (0.01)	0.99	0.94	0.97	0.97	0.93
$\rho(Y,L)$	0.78(0.05)	0.96	0.98	0.99	0.86	

^aThe statistics for the U.S. data are taken from Table 1 in BCF. The model statistics are computed after simulated data have been aggregated to quarterly frequency, logged, and then Hodrick-Prescott filtered.

CD Model

In the third column, the first row reports the volatility of output, which was one of the two calibration targets and is matched fairly well. The volatility of consumption (normalized by that of output) is about 0.4 in the U.S. data, but is overstated at 0.92 in the model. In contrast, investment is too smooth, with a volatility of 1.38 in the model compared to 2.39 in the U.S. data. Although these discrepancies are bothersome, the most glaring shortcoming of the CD model is seen in the behavior of labor hours, which is an order of magnitude too smooth compared to data (0.07 versus 0.80). However, the behavior of the aggregate labor supply masks significant heterogeneity between the two groups' behavior. In particular, labor hours are quite volatile but countercyclical for stockholders $(\sigma(l^h)/\sigma(Y) = 0.77$; correlation with output is -0.96), whereas it is procyclical but smoother for non-stockholders because of their low Frisch labor supply elasticity ($\sigma(l^n)/\sigma(Y) = 0.24$; correlation is +0.97). The behavior of aggregate hours largely mirrors that of non-stockholders (i.e., procyclical and smooth), because they make up a substantial majority of the population. However, aggregate hours are even smoother than that of non-stockholders, exactly because the labor supply of the two groups moves in opposite directions over the business cycle, partly canceling each other. To increase the *volatility* of aggregate hours, one would need to increase the Frisch elasticity of nonstockholders and/or assume a smaller fraction of households to be stockholders. Unfortunately, a higher Frisch elasticity also means a higher EIS for nonstockholders, which contradicts the main empirical evidence this paper builds upon. Because of this important shortcoming, I conclude that Cobb-Douglas utility does not appear to be a promising direction to pursue in this framework for endogenizing labor supply.

Procyclicality of Aggregate Hours

Despite the important shortcomings of the CD model, the procyclical aggregate hours is an encouraging finding, in light of earlier studies that have consistently found that capital adjustment costs create countercyclical hours in representative agent models (cf. BCF and Uhlig (2006)). Thus, it is important to understand why the present model delivers the opposite result. The answer lies in the specific nature of the cross-sectional heterogeneity generated by limited participation. To see why this helps, first note that adjustment costs generate a volatile and procyclical stock price (as in the data). In a representative agent model, such as the one studied by BCF, this implies a large positive wealth effect during expansions, which overcomes the substitution effect from a higher wage rate and causes labor hours to drop during expansions. In contrast, here 80% of the population are non-stockholders and therefore do not experience the described wealth effect. Instead, they mainly respond to the substitution effect of higher wages and increase their labor hours. Although stockholders behave in a similar fashion to the representative agent described

above, they only make up a small fraction of the population. This result therefore suggests that the countercyclical hours found in earlier studies arises from the *interaction* of adjustment costs with the representative agent assumption. By relaxing the latter, the present model is able to generate procyclical hours with Cobb–Douglas preferences.

GHH Model

Turning to the GHH model, the volatility of consumption is lower, whereas the volatility of investment is higher compared to the CD model, and the model is now in the same ballpark as the other two macro-based asset pricing models reported in the table. The more significant improvement is in the volatility of labor hours, where the CD model failed most dramatically: now, the volatility of hours is much higher than before (equal to half the volatility of output) and is closer to the data. This improvement is due to the flexibility afforded by GHH preferences for calibrating the Frisch elasticity independently of the EIS. Aggregate hours (as well as each group's labor hours) are also procyclical, which is due to the lack of wealth effects with GHH preferences. Finally, the fifth column reports the statistics from the GHH model when Frisch elasticity is lowered to 0.5. As seen here, the major impact of this change is a large fall in the volatility of labor hours, which is a major reason why macroeconomic studies typically use higher values as in the baseline calibration. In summary, the macroeconomic implications of GHH preferences are tolerable—that is, comparable to previous macro-based asset pricing models—and are significantly better than the CD model.

6.2. Asset Prices versus Macro Performance: Some Trade-Offs

As noted earlier, there is a fair amount of uncertainty regarding the values of some key model parameters, most notably ξ and α^h . Therefore, I now examine the effect on asset prices and macroeconomic volatilities of varying these two parameters over a plausible range.

I first consider variations in the adjustment cost parameter around its baseline value of 0.4. As ξ is raised from 0.2 to 0.7, it becomes less costly for stockholders to adjust the level of capital installed in the firm, which makes investment a more effective tool for consumption smoothing. The effect can be seen in the right panel of Figure 5 (circles), which plots the combinations of investment volatility and consumption volatility (scaled by output volatility) implied by the model for each value of ξ . The baseline case is marked by the intersection of the dashed horizontal and vertical lines. As ξ rises, investment becomes much more volatile (rises from 1.16 to 2.33) while consumption becomes smoother (from 0.96 to 0.67), bringing both statistics closer to their empirical counterparts (although the lowest volatility figure for consumption is still higher than the 0.40 value in the U.S. data).

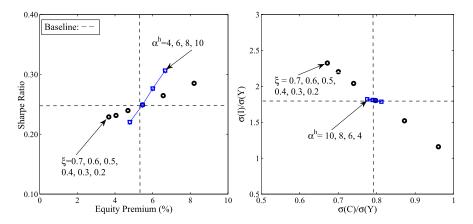


FIGURE 5.—Trade-off between asset prices and macroeconomic volatilities.

Not surprisingly, however, lower adjustment costs and the resulting smoothness of consumption also affect asset prices. This is shown in the left panel, which plots the combinations of equity premium and Sharpe ratio implied by each value of ξ . Raising ξ from 0.2 to 0.7 reduces the equity premium by a factor of about 1.2 (from 8.20% to 3.67%), which is mostly driven by a lower volatility of returns (from 28.1% to 16.1%). As a result, the fall in the Sharpe ratio is a rather small 24% (from 0.285 to 0.229). This comparison suggests that the model's implications for the volatilities of macroeconomic variables can be improved, at the expense of a smaller equity premium and a slightly lower Sharpe ratio.

Next I turn to the risk aversion of stockholders and consider values of α^h from 4 to 10. Starting in the right panel (marked by squares), notice that increasing risk aversion has a very minor impact on the volatilities of investment and consumption (although, *qualitatively*, it moves the model in the right direction). It does, however, have a more significant impact on asset prices (left panel): the equity premium rises from 4.79% to 6.65% with an almost equal rise in the Sharpe ratio (from 0.221 to 0.306).

These two exercises illustrate the trade-offs between the asset pricing and the macroeconomic implications of the model. Together, they suggest that if one is willing to tolerate a risk aversion as high as 10 for stockholders, adjustment costs could be reduced to, for example, $\xi=0.6$. The higher risk aversion would deliver a sizeable equity premium and Sharpe ratio, while the low adjustment cost would move macroeconomic volatilities closer to the data. Nevertheless, a risk aversion of 10 seems quite high, especially for stockholders who are willingly undertaking substantial risks in financial markets.

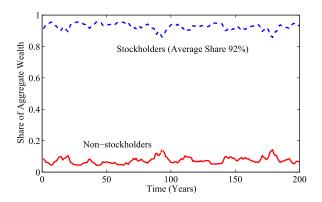


FIGURE 6.—Evolution of wealth distribution over time.

6.3. Distributional Implications

Given the central role played by heterogeneity for the asset pricing results of this paper, an important question to ask is whether the implied cross-sectional behavior is broadly consistent with empirical evidence. I first look at the wealth distribution implied by the GHH model (Figure 6), which reveals substantial inequality between the two groups: on average stockholders own 92% of aggregate wealth, whereas non-stockholders own the remaining 8%. (These shares are fairly robust across specifications: stockholders' share is 86% in the CD model and 89% in the CONS model.) These figures compare fairly well to the U.S. data, where in the 1980s and 1990s stockholders owned an average of 82% of all net worth (fungible wealth, including housing) and more than 90% of financial assets (see Poterba and Samwick (1995) and Guvenen (2006)). As noted above, this implication for wealth inequality is an important difference between the present model and earlier models with limited participation, which required substantial wealth holdings for non-stockholders.

This discussion, however, raises a question of its own: Is the amount of trade in the risk-free asset implied by the model quantitatively plausible, or do we need a substantial amount of trade to sustain the mechanism that generates the equity premium? One way to answer this question is by looking at the trade volume, which I define as the (absolute) change in non-stockholders' bond holdings during a given year compared to the *level* of their bond holdings: $E(|\Delta B|)/E(B)$. This measure is less than 1.1% per year across all versions of the model reported in Tables II and III. This modest figure perhaps does not come as a surprise, given the gradual shifts in the wealth shares shown in Figure 6. As an alternative measure, I compare the size of non-stockholders' *per capita* transactions to their wage income: $E(|B - P^f B'|/(1 - \mu))/E(W)$ is

less than 1.9% annually across all simulations.²⁴ For a non-stockholding household with an annual income of \$50,000, this upper bound implies a net change, for example in their savings account, of \$950 during the year. These relatively small payments entail large changes in stockholders' consumption, because they are synchronized across all non-stockholders (i.e., they result from aggregate shocks) and the effect is concentrated among a small number of stockholders.²⁵

7. CONCLUSIONS

I have studied the implications of a two-agent model with limited stock market participation and heterogeneity in the EIS for asset prices and macroeconomic quantities. My findings suggest that the cross-sectional heterogeneity generated by the interaction of these two features could be important for several macroeconomic and asset pricing phenomena.

The model highlights a new mechanism for the equity premium that results from the limited consumption smoothing opportunities available to the majority of the population, who are non-stockholders. These households turn to the bond market, which effectively transfers their (aggregate) labor income risk and concentrates it among a small group of stockholders. As a result, these households demand to be compensated in the form of a high equity premium. In addition to generating broadly plausible behavior for asset prices, this mechanism is also consistent with the very low wealth holdings of non-stockholders in the U.S. data, which has been problematic for previous models of limited participation. This significant skewness in wealth holdings, in turn, combines with the basic mechanism above to provide a novel explanation for the countercyclicality of the equity premium: essentially, because non-stockholders are very poor and poorly insured, they become effectively more risk averse during recessions when their wealth falls even further. Therefore, stockholders provide more insurance to these agents and bear more risk during these periods. This leads them to demand a higher ex ante premium to hold the equity risk. Another appealing implication of this model is the fairly smooth interest rate process generated by the model despite the very low EIS of the majority of households (non-stockholders). This result is due to the higher EIS of the stockholders who are on the other side of the bond market.

I have also investigated the extent to which the labor supply decision can be endogenized in this framework. Cobb-Douglas utility gave rise to some counterfactual implications and therefore did not seem to offer a promising

²⁴To construct the measure, I first annualize the total transactions by adding up $B_t - P_t^f B_{t+1}$ over 12 consecutive months and then take the absolute value. If I instead take the absolute value of monthly transactions first and then add up, the reported figure changes very little: it rises from 1.9% to 1.97%.

²⁵To see this, note that $E(|B - P^f B'|/\mu)/E(Cs) = 4.9\%$.

direction. In contrast, GHH preferences did not cause deterioration in asset pricing implications compared to the inelastic labor case. At the same time, the model's implications for some key business cycle statistics, such as the volatilities of consumption and investment, need improvement. Therefore, the present model makes only modest progress in tackling these well-known short-comings shared by many macro-based asset pricing models.

A limitation of the present model is that it abstracts from long-run growth. Essentially, I assume that the economy is stationary in levels to circumvent the difficulties associated with obtaining a stationary wealth distribution with preference heterogeneity and long-run growth. Chan and Kogan (2002) were able to generate a stationary wealth distribution by introducing "benchmark consumption levels" into preferences. Although incorporating a similar idea into this framework would be a valuable extension, this is beyond the scope of the present analysis and remains an important area for expanding this model.

Finally, there are many parallels between the asset pricing results of this paper and those obtained in the external habit model of Campbell and Cochrane (1999). It turns out that these similarities point to a deeper connection between the two frameworks: indeed, the limited participation model studied in this paper has a reduced form representation that is very similar to Campbell and Cochrane's model, where the "external habit stock" in their framework corresponds to the consumption of non-stockholders in the present model. However, these similarities do not extend to the macroeconomic and policy implications of the two models, so the limited participation model should not be interpreted as providing microfoundations for the particular habit specification used by these authors. These links between the two frameworks are explored in detail in Guvenen (2009).

I hope that these results will also encourage further research on the reasons behind limited participation, which is not addressed in this paper.²⁶ Furthermore, given the central role played by limited participation in this model, another important research avenue is to investigate the consequences of the recent trends in participation observed in most countries for asset prices as well as for wealth inequality and welfare.

²⁶Recently, Gomes and Michaelides (2008) constructed a life-cycle model where individuals pay a one-time fixed cost to become a stockholder and argued that in this setting limited participation has a much smaller impact on asset prices. Their conclusion does not follow from the endogeneity of participation per se, because one can introduce a one-time cost into the present framework and show that it results in individuals with high EIS to enter the stock market whereas those with low EIS stay out. With a cost of appropriate magnitude, the resulting equilibrium is identical to the one studied here. (Further calculations on this fixed cost are available upon request.) The difference instead appears to come from some of the calibration choices made by these authors.

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Manuscript received August, 2006; final revision received August, 2009.